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Lower Bound on the Pseudoscalar Mass in the Minimal Supersymmetric Standard Model

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Abstract

In the Higgs sector of the Minimal Supersymmetric Standard Model, the mass of the pseudoscalar A is an independent parameter together with $\tan\beta \equiv v_2/v_1$. If m_A is small, then the process $e^+e^- \to h + A$ is kinematically allowed and is suppressed only if $\tan\beta$ is small. On the other hand, the mass of the charged Higgs boson is now near M_W, and the decay $t \to b + h^+$ is enhanced if $\tan\beta$ is small. Since the former has not been observed, and the branching fraction of $t \to b + W$ cannot be too small (by comparing the experimentally derived $t\bar{t}$ cross section from the leptonic channels with the theoretical prediction), we can infer a phenomenological lower bound on m_A of at least 60 GeV for all values of $\tan\beta$.

The most studied extension of the standard $SU(2) \times U(1)$ electroweak gauge model is that of supersymmetry with the smallest necessary particle content. In this Minimal Supersymmetric Standard Model (MSSM), there are two scalar doublets $\Phi_1 = (\phi_1^+, \phi_1^0)$ and $\Phi_2 = (\phi_2^+, \phi_2^0)$, with Yukawa interactions $\overline{(u,d)}_L d_R \Phi_1$ and $\overline{(u,d)}_L u_R \tilde{\Phi}_2$, respectively, where $\tilde{\Phi}_2 = i\sigma_2 \Phi_2^* = (\overline{\phi_2^0}, -\phi_2^-)$. The Higgs sector of the MSSM has been studied in great detail[1] and it is a current topic of intensive experimental and theoretical scrutiny.[2] There are five physical Higgs bosons in the MSSM: two neutral scalars (h and H), one neutral pseudoscalar (A), and two charged ones ($h^\pm$). Their masses and couplings to other particles are completely determined up to two unknown parameters which are often taken to be m_A and $\tan\beta \equiv v_2/v_1$, where v_i is the vacuum expectation value of ϕ_i^0.

In the following, we will show that $m_A > 60$ GeV for all values of $\tan\beta$. Our conclusion is based on a combination of theoretical and experimental inputs from a number of different observations which have become available recently.

In the MSSM, the pseudoscalar Higgs boson A and the charged Higgs bosons $h^\pm$ are given by analogous expressions, namely

$$\begin{aligned} A &= \sqrt{2}(\sin\beta \mathrm{Im}\phi_1^0 - \cos\beta \mathrm{Im}\phi_2^0), & (1)\\ h^\pm &= \sin\beta \phi_1^\pm - \cos\beta \phi_2^\pm. & (2) \end{aligned}$$

At tree level, their masses are related by $m_{h^\pm}^2 = m_A^2 + M_W^2$. The mass-squared matrix spanning the two neutral scalar Higgs bosons $\sqrt{2}\mathrm{Re}\phi_{1,2}^0$ is given by

$$\mathcal{M}^2 = \begin{bmatrix} m_A^2 \sin^2\beta + M_Z^2 \cos^2\beta & -(m_A^2 + M_Z^2)\sin\beta\cos\beta \\ -(m_A^2 + M_Z^2)\sin\beta\cos\beta & m_A^2\cos^2\beta + M_Z^2\sin^2\beta + \epsilon/\sin^2\beta \end{bmatrix}. \quad (3)$$

In the above, ϵ is the leading radiative correction[6] due to the t quark:

$$\epsilon = \frac{3g_2^2 m_t^4}{8\pi^2 M_W^2} \ln\left(1 + \frac{\tilde{m}^2}{m_t^2}\right), \quad (4)$$

where $\tilde{m}$ is the mass parameter for the supersymmetric scalar quarks.

Let us take $m_A = 0$ and rotate $\mathcal{M}^2$ to the basis spanned by

$$h_1 = \sqrt{2}(\sin\beta \mathrm{Re}\phi_1^0 - \cos\beta \mathrm{Re}\phi_2^0), \quad h_2 = \sqrt{2}(\cos\beta \mathrm{Re}\phi_1^0 + \sin\beta \mathrm{Re}\phi_2^0). \tag{5}$$

We get[3]

$$\mathcal{M}^2 = \left[\begin{array}{cc} M_Z^2 \sin^2 2\beta + \epsilon \cot^2\beta & -M_Z^2 \sin 2\beta \cos 2\beta + \epsilon \cot\beta \\ -M_Z^2 \sin 2\beta \cos 2\beta + \epsilon \cot\beta & M_Z^2 \cos^2 2\beta + \epsilon \end{array} \right]. \tag{6}$$

It is well-known that in this basis, the h_1ZZ and h_2AZ couplings are absent, hence the nonobservation of $e^+e^- \to h+A$ does not rule out any value of m_A if $\tan\beta$ is small enough[4]. In this limit, the eigenstates of $\mathcal{M}^2$ are essentially h_1 and h_2. If $h \simeq h_1$, then it is too heavy to be produced. If $h \simeq h_2$, then its coupling to A is too small to have a measurable branching fraction. Note that $\epsilon \simeq M_Z^2$, *i.e.* (91 GeV)^2, for $m_t = 175$ GeV and $\tilde{m} = 1$ TeV.

From the nonobservation of $e^+e^- \to h + Z$ where the Z boson may be either real or virtual and the nonobservation of $e^+e^- \to h + A$, where h is an arbitrary linear combination of h_1 and h_2, it is possible to obtain the MSSM exclusion region in the $m_A - \tan\beta$ plane. One such detailed analysis[5] using only LEP1 data collected at the Z resonance shows that m_A has to be greater than about $M_Z/2$ for $\tan\beta > 1$. With the higher energies available at LEP2 since then, this bound is expected to be at least 60 GeV.

To obtain a lower bound on m_A for $\tan\beta < 1$, we propose to use the MSSM relationship[6]

$$m_{h^\pm}^2 = m_A^2 + M_W^2 - \frac{\epsilon}{4\sin^2\beta}\frac{M_W^2}{m_t^2}, \tag{7}$$

where the last term is the leading radiative correction for $\tan\beta < 1$. We then derive bounds on m_A from the bounds on $m_{h^\pm}$ by considering t decay. Taking $m_t = 175$ GeV, we see that $t \to b + h^+$ is allowed for values of $m_{h^\pm}$ up to 170 GeV, corresponding to m_A up to about 150 GeV. The nonobservation of the above process would then translate into lower bounds on m_A as a function of $\tan\beta$.

In the MSSM, the charged-Higgs-boson couplings to the quarks and leptons are given by

$$\mathcal{H}_{int} = \frac{-g_2}{\sqrt{2}M_W} h^+ [\cot\beta \; m_{u_i} \bar{u}_i d_{iL} + \tan\beta \; m_{d_i} \bar{u}_i d_{iR} + \tan\beta \; m_{l_i} \bar{\nu}_i l_{iR}] + h.c., \tag{8}$$

where the subscript i represents the generation index, and we have used the diagonal KM matrix approximation[7]. The leading-logarithm QCD (quantum chromodynamics) correction is taken into account by substituting the quark mass parameters by their running masses evaluated at the $h^\pm$ mass scale. The resulting decay widths are

$$\Gamma(t \to bh^+) = \frac{g_2^2 \lambda^{1/2}(1, m_b^2/m_t^2, m_{h^+}^2/m_t^2)}{64\pi M_W^2 m_t} [(m_t^2 \cot^2\beta + m_b^2 \tan^2\beta)(m_t^2 + m_b^2 - m_{h^+}^2) - 4m_t^2 m_b^2], \tag{9}$$

where λ denotes the usual Kallen function and $\lambda^{1/2}$ is equal to the magnitude of the momentum of either decay product divided by $m_t/2$, and

$$\begin{aligned} \Gamma(h^+ \to \tau^+\nu) &= \frac{g_2^2 m_{h^+}}{32\pi M_W^2} m_\tau^2 \tan^2\beta, & (10) \\ \Gamma(h^+ \to c\bar{s}) &= \frac{3g_2^2 m_{h^+}}{32\pi M_W^2} (m_c^2 \cot^2\beta + m_s^2 \tan^2\beta). & (11) \end{aligned}$$

Assuming that the only other competing channel is the standard-model decay $t \to bW^+$, the $t \to bh^+$ branching fraction is then

$$B = \frac{\Gamma(t \to bh^+)}{\Gamma(t \to bh^+) + \Gamma(t \to bW^+)}, \tag{12}$$

where

$$\Gamma(t \to bW^+) = \frac{g_2^2 \lambda^{1/2}(1, m_b^2/m_t^2, M_W^2/m_t^2)}{64\pi M_W^2 m_t} [M_W^2(m_t^2 + m_b^2) + (m_t^2 - m_b^2)^2 - 2M_W^4]. \tag{13}$$

It is clear from Eq. (9) that B has a minimum at $\tan\beta = (m_t/m_b)^{1/2} \simeq 6$, but it becomes large for $\tan\beta < 1$ and $\tan\beta > m_t/m_b$. Thus we expect to see a sizeable $t \to bh^+$ signal in these two regions if $m_{h^+} < m_t$.

We see from Eqs. (10) and (11) that $\tau^+\nu$ is the dominant decay mode of h^+ if $\tan\beta >> 1$. Thus an excess of $t\bar{t}$ events in the τ channel compared to the standard-model prediction constitutes a viable $h^{\pm}$ signal in the large $\tan\beta$ region. A recent analysis[8] of the CDF $t\bar{t}$ data in the τl channel ($l = e, \mu$) has led to a mass bound of $m_{h^{\pm}} > 100$ GeV for $\tan\beta > 40$. A similar bound has also been obtained from the same $t\bar{t}$ data in the inclusive τ channel[9].

The above method is not applicable in the small $\tan\beta$ region, where h^+ is expected to decay mainly into $c\bar{s}$, *i.e.* two jets. On the other hand, we can use the so-called disappearance method to look for the presence of $t \to bh^+$ decay in both the small and large $\tan\beta$ regions[7] as described below. The key observation is that $h^{\pm}$ couples negligibly to the light fermions, particularly e and μ, whereas the W boson couples to them with full strength universally. Since the e and μ decay modes play an important role in the detection of $t\bar{t}$ events at the Tevatron, the experimentally derived $t\bar{t}$ cross section is sensitive to the branching fraction B of Eq. (12). After all, if t decays into bh^+, there would not be any energetic e or μ in the final state, as would be possible with the W boson.

The experimental $t\bar{t}$ cross sections obtained by the CDF and D0 collaborations[10, 11] are weighted averages of their measured cross sections in the (I) dilepton (ll) and (II) lepton plus multijet (lj) channels, using the standard formula

$$\sigma = \frac{\Sigma(\sigma_i/\delta_i^2)}{\Sigma(1/\delta_i^2)}. \tag{14}$$

They are summarized below.

$$\mathrm{CDF}: \quad \sigma_{ll} = 8.5 \begin{array}{c} +4.4 \\ -3.4 \end{array} \mathrm{pb}, \quad \sigma_{lj} = 7.2 \begin{array}{c} +2.1 \\ -1.7 \end{array} \mathrm{pb} \quad \Rightarrow \quad \sigma_{\mathrm{CDF}} = 7.5 \begin{array}{c} +1.9 \\ -1.6 \end{array} \mathrm{pb}. \tag{15}$$

$$\mathrm{D0}: \quad \sigma_{ll} = 6.3 \pm 3.3 \ \mathrm{pb}, \quad \sigma_{lj} = 5.1 \pm 1.9 \ \mathrm{pb} \quad \Rightarrow \quad \sigma_{\mathrm{D0}} = 5.5 \pm 1.8 \ \mathrm{pb}. \tag{16}$$

The σ_{lj} of CDF is a weighted average of the measured cross sections using the SVX and SLT b-tagging methods; that of D0 is a weighted average of those using kinematic cuts and SLT b-tagging. In both cases, the weight of the SLT method is rather low. From Eqs. (15) and (16), we see that for both CDF and D0, $\delta_{lj} \simeq \delta_{ll}/2$, hence

$$\sigma \simeq \frac{\sigma_{ll} + 4\sigma_{lj}}{5}. \tag{17}$$

Furthermore, since the CDF and D0 cross sections have essentially identical errors, we can take a simple average of the two:

$$\sigma_{\mathrm{CDF+D0}} = 6.5 \begin{array}{c} +1.3 \\ -1.2 \end{array} \mathrm{pb}. \tag{18}$$

Here we have combined the two errors using $\delta^{-2} = \delta_1^{-2} + \delta_2^{-2}$, since they are largely statistical.

We note that the dilepton channel (I) corresponds to the leptonic (e, μ) decay of both the t and $\bar{t}$ quarks, whereas the lepton plus multijet channel (II) corresponds to the leptonic decay of one, say $t \to bl^+\nu$, and the hadronic decay of the other. For the standard-model decay $t \to bW^+$, the respective branching fractions are 2/9 and 2/3, whereas for the postulated decay $t \to bh^+$, they are 0 and a function which rises rapidly to 1 for $\tan\beta < 1$. Thus the relative contributions of different final states to the two channels are $WW : Wh^{\pm} : h^{\pm}h^{\mp} = 1 : 0 : 0$ for (ll) and $1 : 3/4 : 0$ for (lj). [We have used the maximum value of 3/4 corresponding to very small $\tan\beta$. This is a conservative approach, because any smaller value will give us a better bound on $m_{h^{\pm}}$ as explained below.] We have then a suppression factor relative to the standard model of

$$f_{ll} = (1 - B)^2 \simeq 0.5 \quad (\text{for } B = 0.3), \tag{19}$$

$$f_{lj} = (1 - B)^2 + 2B(1 - B)(3/4) \simeq 0.8 \quad (\text{for } B = 0.3). \tag{20}$$

Since the relative weights of the (ll) and (lj) channels are 1:4, Eqs. (19) and (20) correspond to an effective suppression factor of

$$f = 0.74 \quad (\text{for } B = 0.3). \tag{21}$$

We note that for large $\tan\beta$, $h^{\pm}$ decays mainly into τ, hence it would be hard for the $Wh^{\pm}$ final state to pass the $n_{\mathrm{jet}} \geq 3$ cut required for the (lj) channel. This implies an extra suppression factor of about 1/3 for the $Wh^{\pm}$ contribution, hence f is about 0.7 already for $B = 0.2$, *i.e.* our bound is conservative because it assumes $B = 0.3$.

Finally the theoretical estimates of the $t\bar{t}$ cross section including higher-order QCD corrections are 4.13 to 5.48 pb[12], and 5.10 to 5.59 pb[13]. These ranges are not identical, but the two estimates are in reasonable agreement as to their upper bounds. We shall thus assume for our purpose that

$$\sigma(t\bar{t}) \leq 5.6 \text{ pb}. \tag{22}$$

Combining this with the suppression factor of Eq. (21), we obtain an upper bound of

$$\sigma \leq 4.1 \text{ pb} \tag{23}$$

for the weighted cross section of Eq. (17). This is 2σ lower than the combined CDF and D0 estimate of Eq. (18), as well as the CDF estimate of Eq. (15). Hence we can take $B = 0.3$ as a 2σ upper bound for the branching fraction of $t \to bh^+$ decay. In Figure 1 we plot the exclusion regions of $m_{h^\pm}$ as a function of $\tan\beta$ using $B = 0.3$. We also show the exclusion region obtained in Ref. [8], which used the "appearance" method of looking for τ, instead of the "disappearance" method of not finding e or μ discussed here.

To convert a bound on $m_{h^\pm}$ to one on m_A, we use the full expression including all one-loop radiative corrections[6] in place of Eq. (7) which is approximate and valid only for $\tan\beta < 1$. In Figure 2 we plot the exclusion regions of m_A as a function of $\tan\beta$ deduced from t decay and $t\bar{t}$ production corresponding to Fig. 1. We note that the radiative correction is negative for small $\tan\beta$ which increases the m_A bound, and is positive for large $\tan\beta$ which decreases it. We note also that at extreme values of $\tan\beta$, near 0.2 and 100, the Yukawa couplings involved are becoming too large for a perturbative calculation to be reliable. We then add a line at $m_A = 60$ GeV for $\tan\beta > 1$ as a conservative upper limit from the combined LEP data[5, 14]. Our conclusion is simple: in the Minimal Supersymmetric Standard Model, combining what we know from LEP and the Tevatron and using a conservative estimate of the theoretical $t\bar{t}$ cross section, the pseudoscalar mass m_A is now known to be greater than 60 GeV for all values of $\tan\beta$.

Note Added: After the completion of our paper, we found out that the ALEPH Collaboration has just recently obtained[15] the bound $m_A > 62.5$ GeV for $\tan\beta > 1$.

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References

[1] See for example J. F. Gunion, H. E. Haber, G. Kane, and S. Dawson, *The Higgs Hunters' Guide* (Addison-Wesley, Reading, MA, 1990).

[2] For a recent review, see for example H. E. Haber, hep-ph/9707213.

[3] See for example T. V. Duong, E. Keith, E. Ma, and H. Kikuchi, Phys. Rev. **D52**, 5045 (1995).

[4] See for example E. Ma and D. Ng, Phys. Rev. **D49**, 6164 (1994).

[5] J. Rosiek and A. Sopczak, Phys. Lett. **B341**, 419 (1995).

[6] For a review of radiative corrections, see for example H. E. Haber, R. Hempfling, and A. H. Hoang, hep-ph/9609331.

[7] See for example R. M. Godbole and D. P. Roy, Phys. Rev. **D43**, 3640 (1991); M. Drees and D. P. Roy, Phys. Lett. **B269**, 155 (1991).

[8] M. Guchait and D. P. Roy, Phys. Rev. **D55**, 7263 (1997).

[9] CDF Collaboration: F. Abe *et al.*, Phys. Rev. Lett. **79**, 357 (1997).

[10] CDF Collaboration: D. W. Gerdes, hep-ex/9706001, Report No. Fermilab-Conf-97-166-E, to appear in *Proc. of XXXII Rencontres de Moriond on Electroweak Interactions and Unified Theories*, Les Arcs, France, March 1997.

[11] D0 Collaboration: S. Abachi *et al.*, hep-ex/9704015, Report No. Fermilab-Pub-97-109-E (submitted to Phys. Rev. Lett.)

[12] S. Catani *et al.*, Phys. Lett. **B378**, 329 (1996).

[13] E. Berger and H. Contopanagos, Phys. Rev. **D54**, 3085 (1996).

[14] A detailed updated analysis (A. Sopczak, private communications) shows that the m_A bound is actually much higher than 60 GeV.

[15] The ALEPH Collaboration, R. Barate *et al.*, Report No. CERN-PPE/97-071 (June 1997).

Figure Captions

Fig. 1. Exclusion regions at 95% confidence level in the $m_{h^\pm} - \tan\beta$ plane using $B = 0.3$ (solid lines) for $t \to bh^+$ as explained in the text. The dashed line corresponds to the method used in Ref. [8].

Fig. 2. Exclusion regions at 95% confidence level in the $m_A - \tan\beta$ plane. Regions I and III correspond to those depicted in Fig. 1 with $m_{h^\pm}$ converted to m_A taking into account the MSSM one-loop radiative corrections. Region II represents a conservative estimate of the expected limit from LEP1 and LEP2 for $\tan\beta > 1$ (dotted line). A slightly higher value of 62.5 GeV for $\tan\beta > 1$ has just recently been obtained by the ALEPH Collaboration[15].

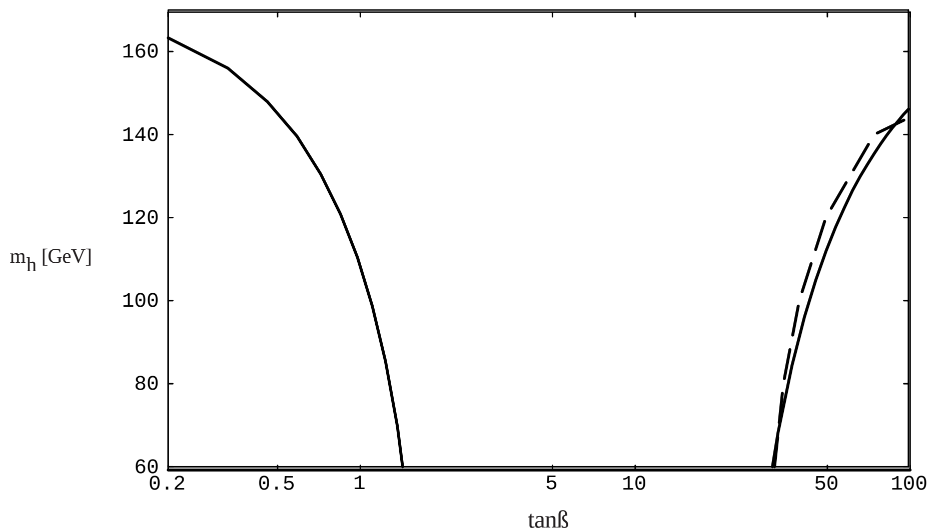
160
140
120
100
80
60
m_h [GeV]
0.2
0.5
1
5
10
50
100
tanß

Fig. 1

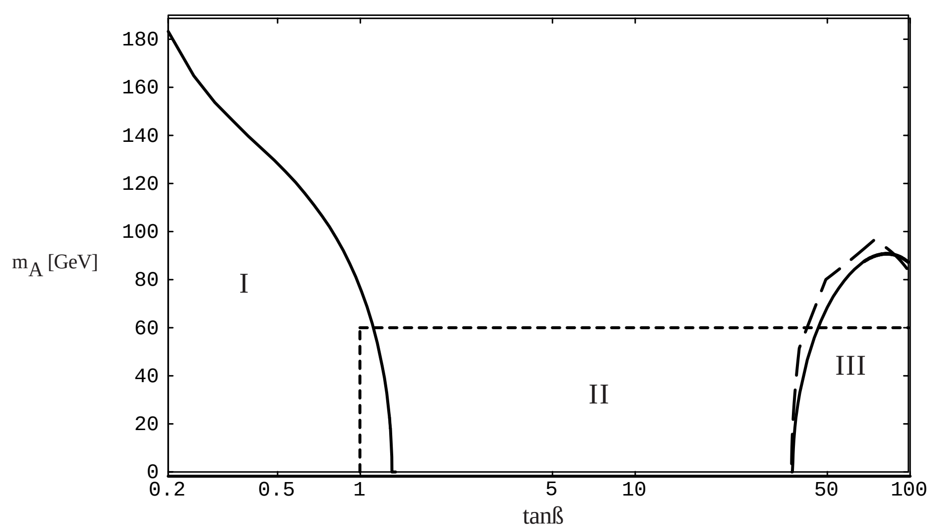
180
160
140
120
100
80
60
40
20
0
m_A [GeV]
I
II
III
0.2
0.5
1
5
10
50
100
tanß

Fig. 2